

# Self-Consistent Trajectory Autoencoder: Hierarchical Reinforcement Learning with Trajectory Embeddings

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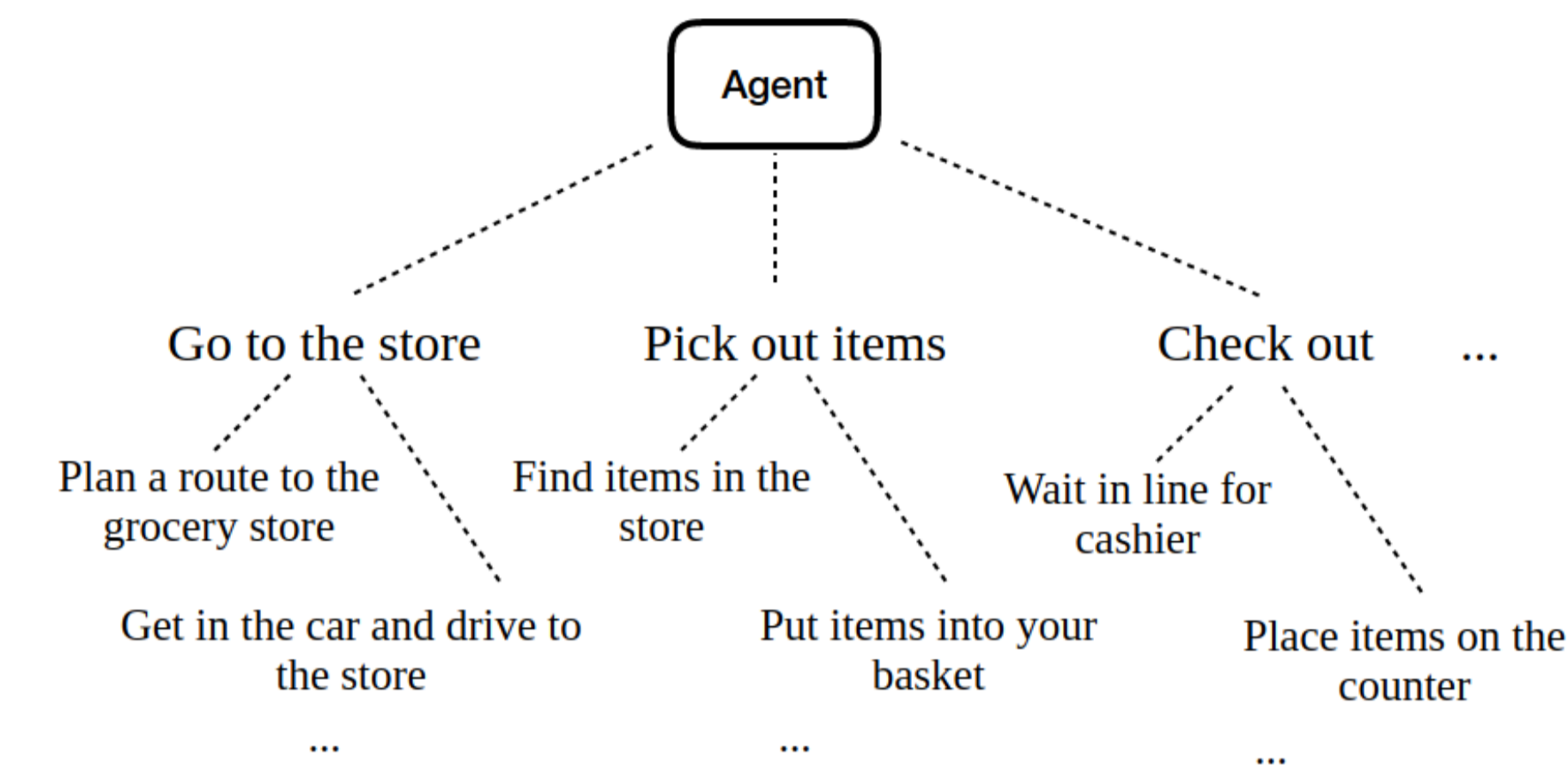
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## Motivation

**Problem:** Solve long horizon or sparse reward tasks by learning temporally abstract lower-level skills for hierarchical reinforcement learning. Example: Grocery shopping



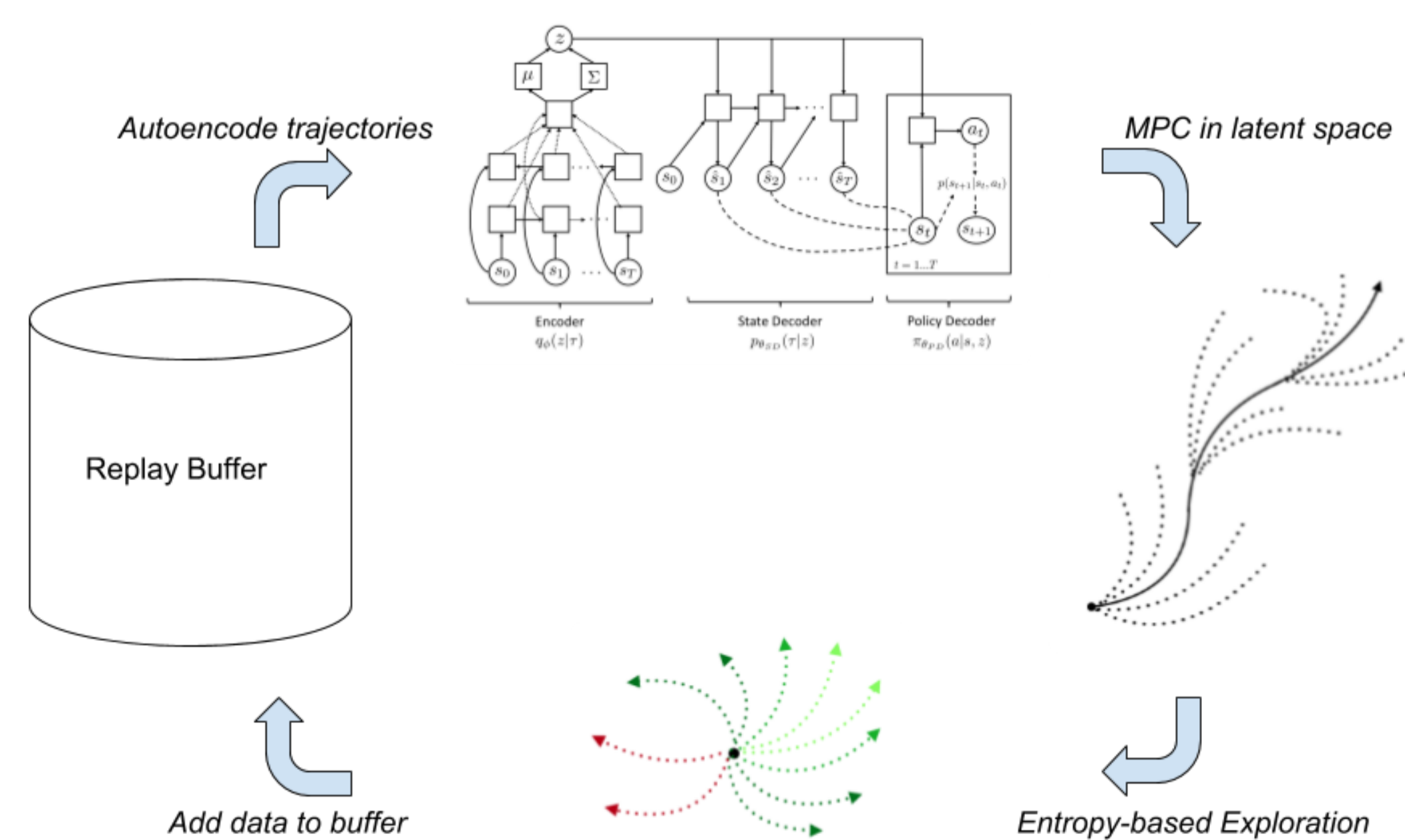
## Hierarchical RL:

- ▶ Decompose task into easier problems.
- ▶ Reason in terms of abstract low-level skills instead of single actions.
- ▶ High level abstraction enables temporally extended planning.

## Challenges

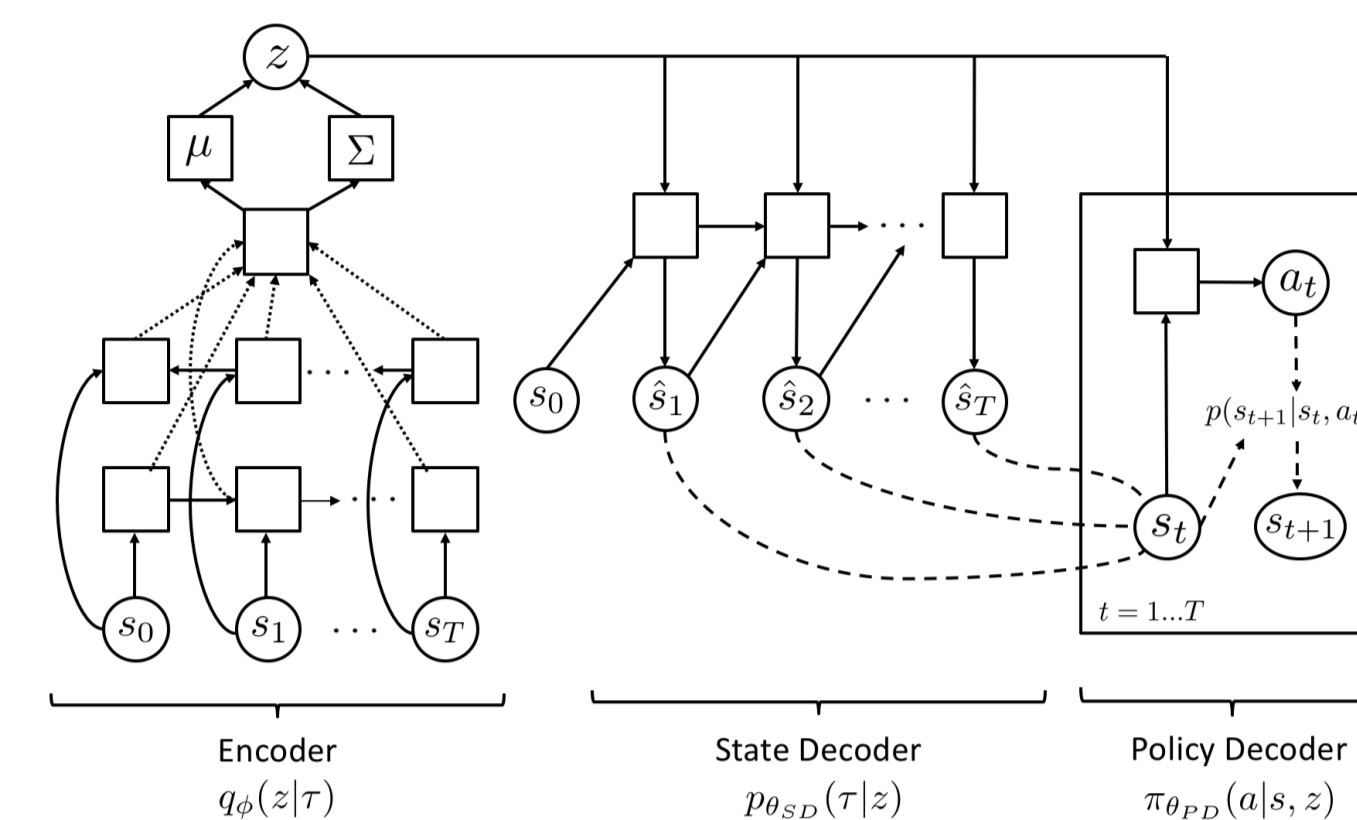
- ▶ Representations for lower-level skills
  - ▶ **Previous:** Discrete options: Sutton et al., 1999, Bacon et al., 2017
  - ▶ **Ours** → Continuous representation of skills
- ▶ Learning lower-level skills
  - ▶ **Previous:** Hand specified objectives: Florensa et al. 2017; Sutton et al., 1999
  - ▶ **Ours** → Generic objectives.
- ▶ Planning over long time-horizons
  - ▶ **Previous:** Model Predictive Control: Nagabadi et al., 2017
  - ▶ **Ours** → Model closed-loop behavior over entire trajectories.

## Method Overview



- ▶ Learn continuous representation of lower-level skills with trajectory VAE.
- ▶ Learn diverse set of skills using maximum entropy exploration.
- ▶ High-level planning in space of learned skills with MPC.

## Self-Consistent Trajectory Autoencoder



## Graphical Model

- ▶ Encoder  $q_\phi(z | \tau)$  encodes trajectory into latent distribution.
- ▶ State Decoder  $p_{\theta_{SD}}(\tau | z)$  decodes  $z$  into sequence of states.
- ▶ Policy Decoder  $p_{\theta_{PD}}(a | s, z)$  conditions on  $z$  to produce same trajectory in environment.

## Optimization

$$\max \log p(\tau) \\ \text{subject to } \mathbb{E}_{q_\phi} [D_{KL}(p_{\theta_{PD}}(\tau | z) \| p_{\theta_{SD}}(\tau | z))] = 0$$

- ▶ Maximize likelihood of trajectory data while ensuring state decoder and policy decoder are consistent.

$$\mathbb{E}_{q_\phi} [\log p_{\theta_{SD}}(\tau | z)] - D_{KL}(q_\phi(z | \tau) \| p(z)) + \lambda [\mathbb{E}_{q_\phi, p_{\theta_{PD}}}(\tau | z) [\log p_{\theta_{SD}}(\tau | z) + \mathcal{H}(p_{\theta_{PD}}(\tau | z))] ]$$

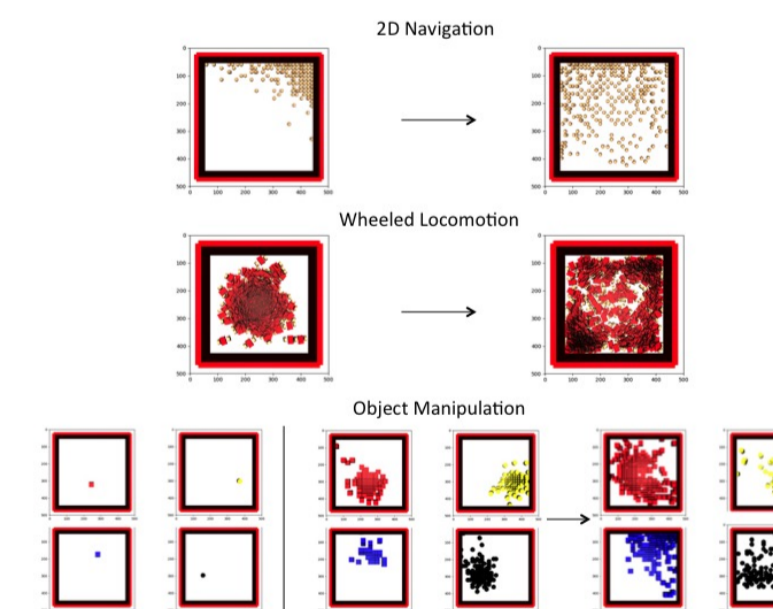
Maximum Entropy RL

- ▶ Train state decoder with supervised learning, policy decoder with RL

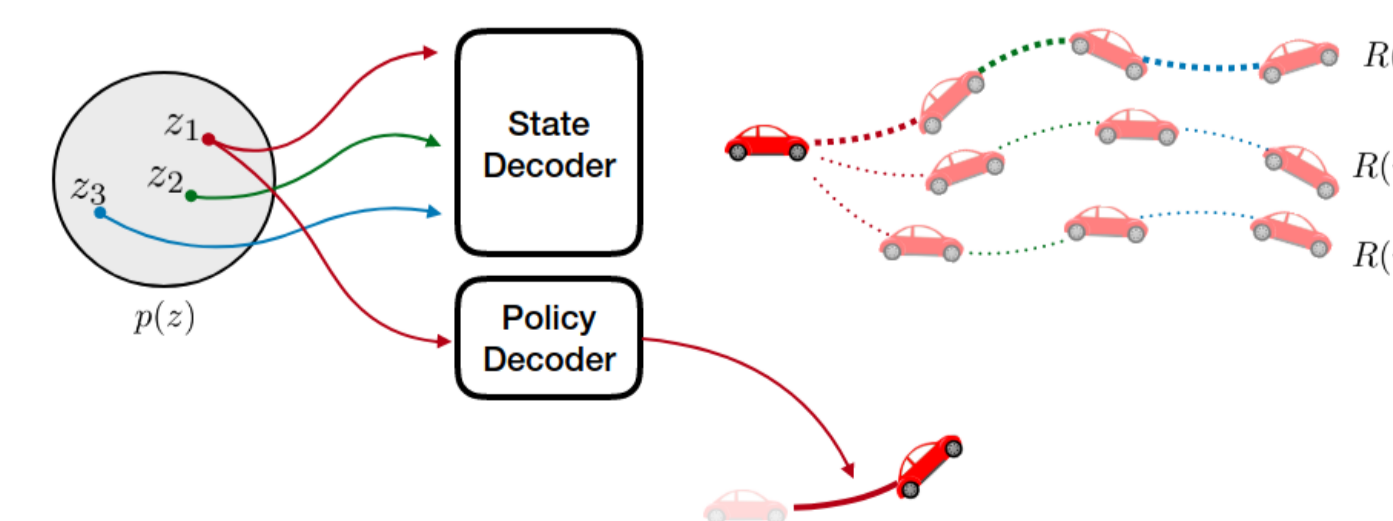
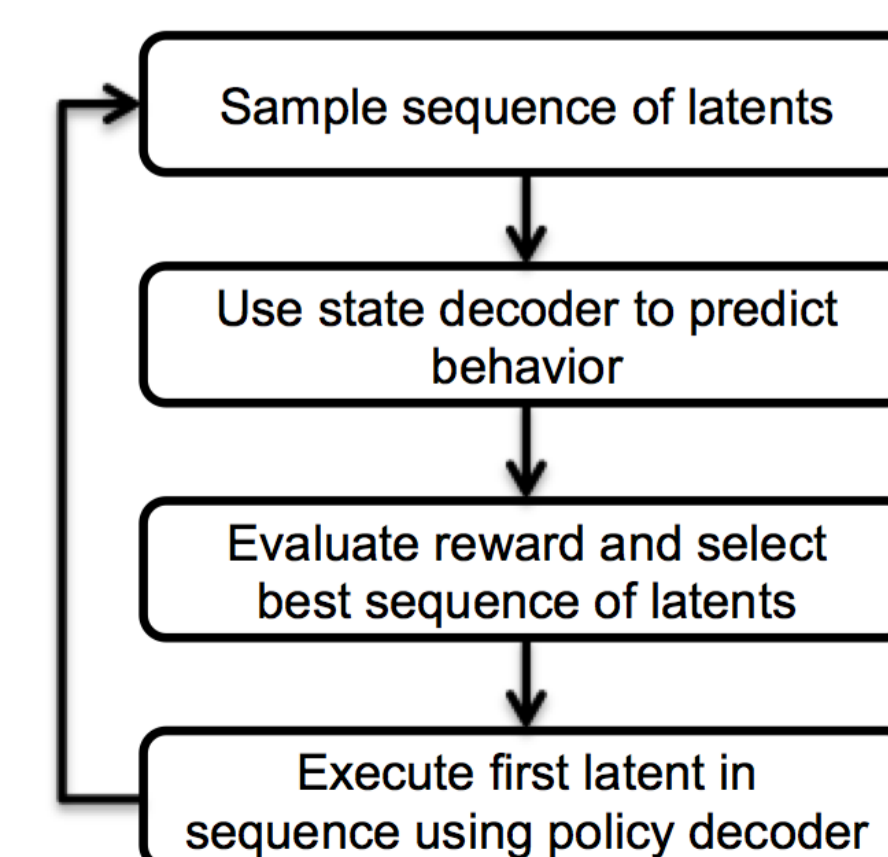
## Learn Diverse Set of Skills

- ▶ Encourage diverse behavior by maximizing marginal entropy over trajectories

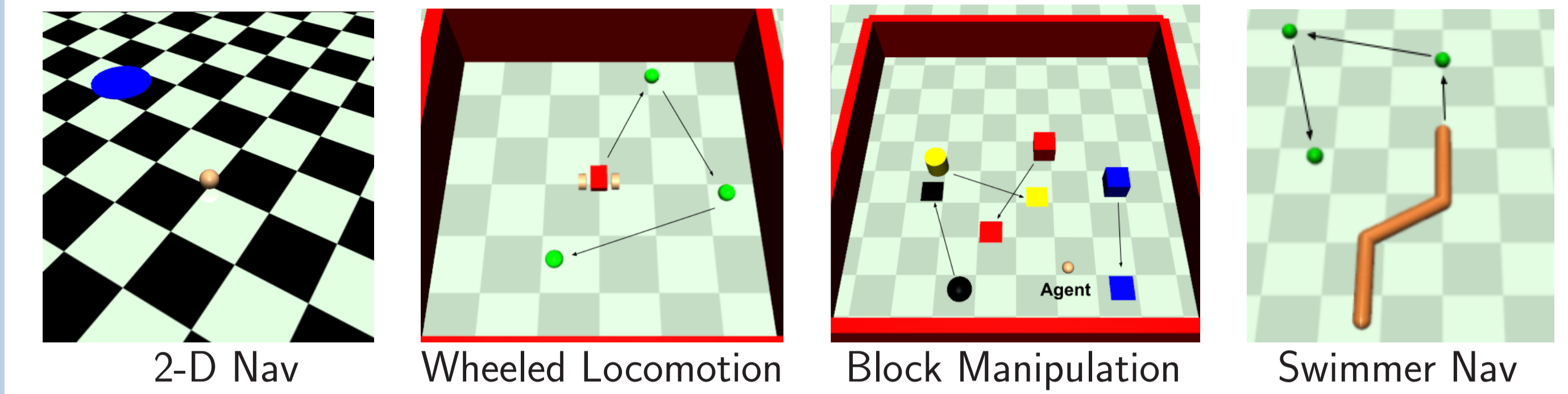
$$\max_{\theta} \mathcal{H}(p_{\theta}(\tau)) = -\mathbb{E}_{p_{\theta}(\tau)} [\log p_{\theta}(\tau)]$$



## Hierarchical Control

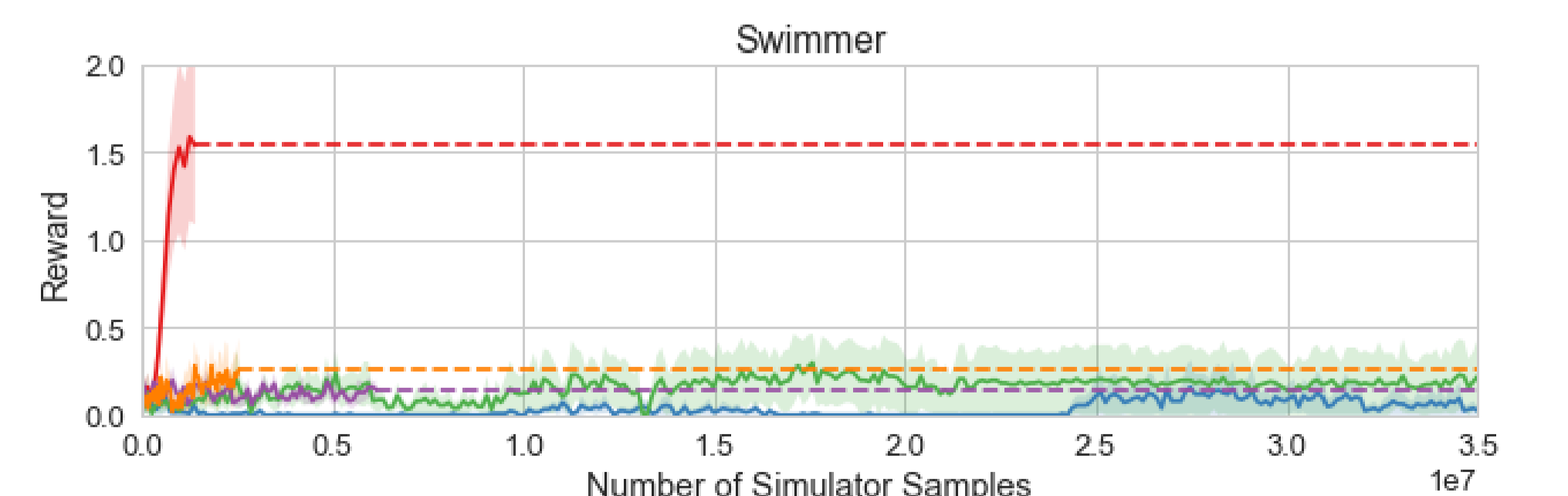
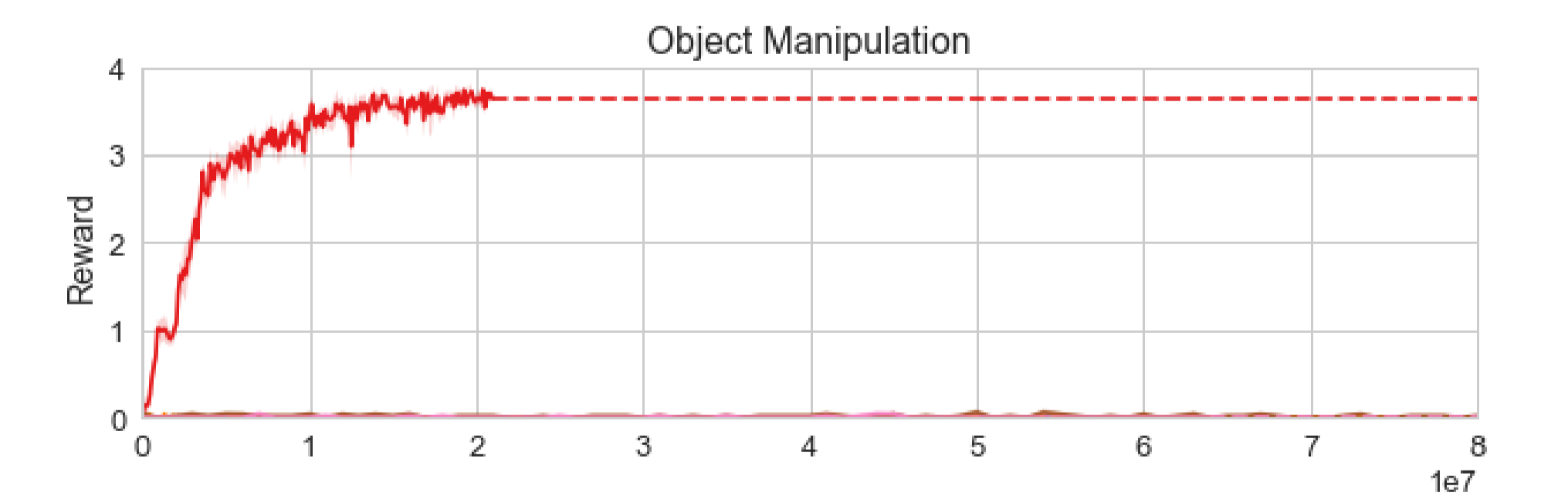
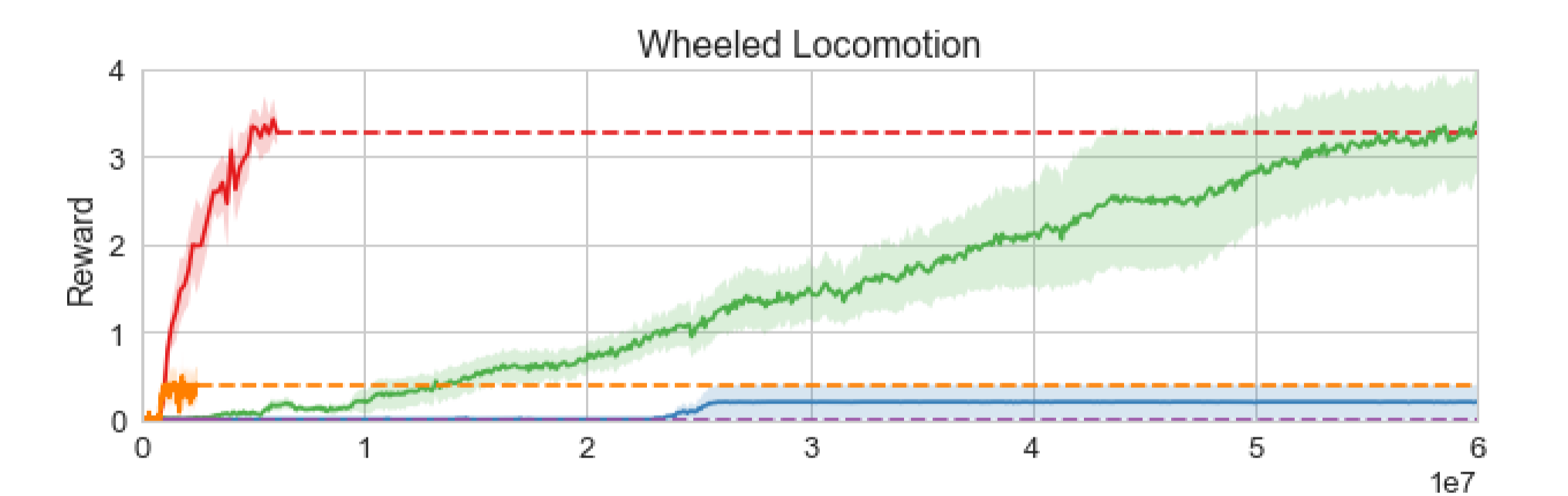
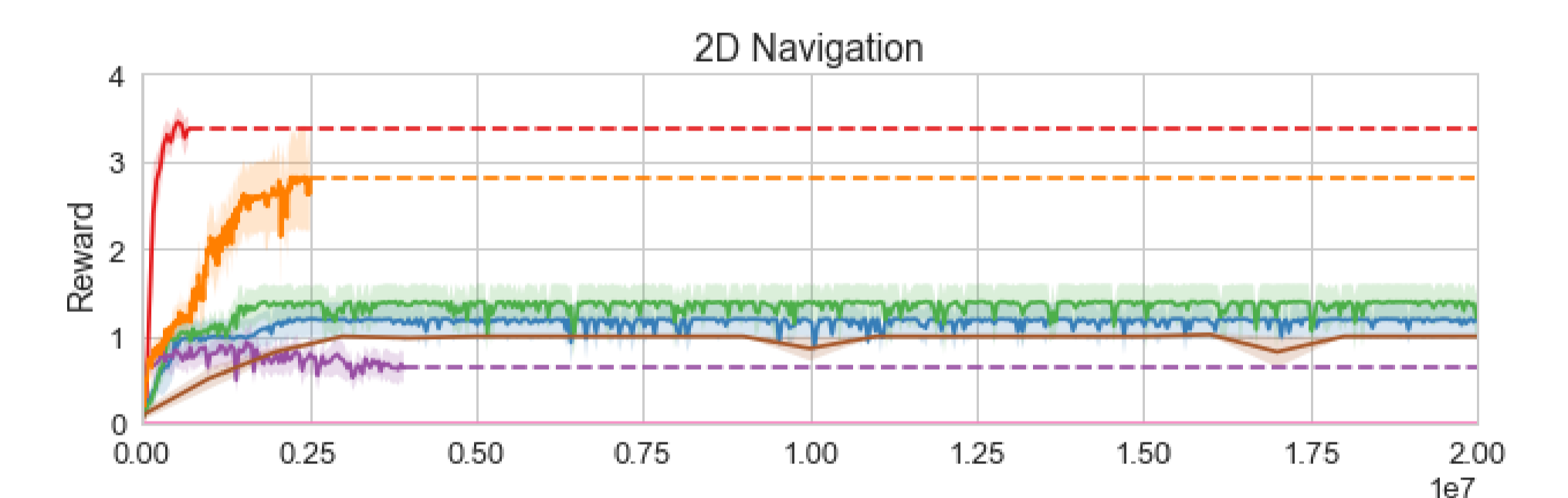


## Experimental Results



Tasks:

- ▶ **2-D Navigation:** Navigate a specific sequence of waypoints with reward every 3rd waypoint. Long horizon task with sparse rewards.
- ▶ **Wheeled Locomotion:** Navigate a wheeled robot through a series of goals. Tests reasoning over continuous action space.
- ▶ **Block Manipulation:** Pick up blocks and move them to the correct goal locations. Model must explore and learn useful interaction skills with objects.
- ▶ **Swimmer Navigation:** Navigate through a series of waypoints with a 3-link robotic swimmer. Must acquire low-level swimming gait and higher-level navigation strategy.



— Ours — MPC — A3C — TRPO — Option Critic — VIME — FeUdal

Video results online: <https://sites.google.com/view/sectar/home>